

# Module 12

## Machine Learning

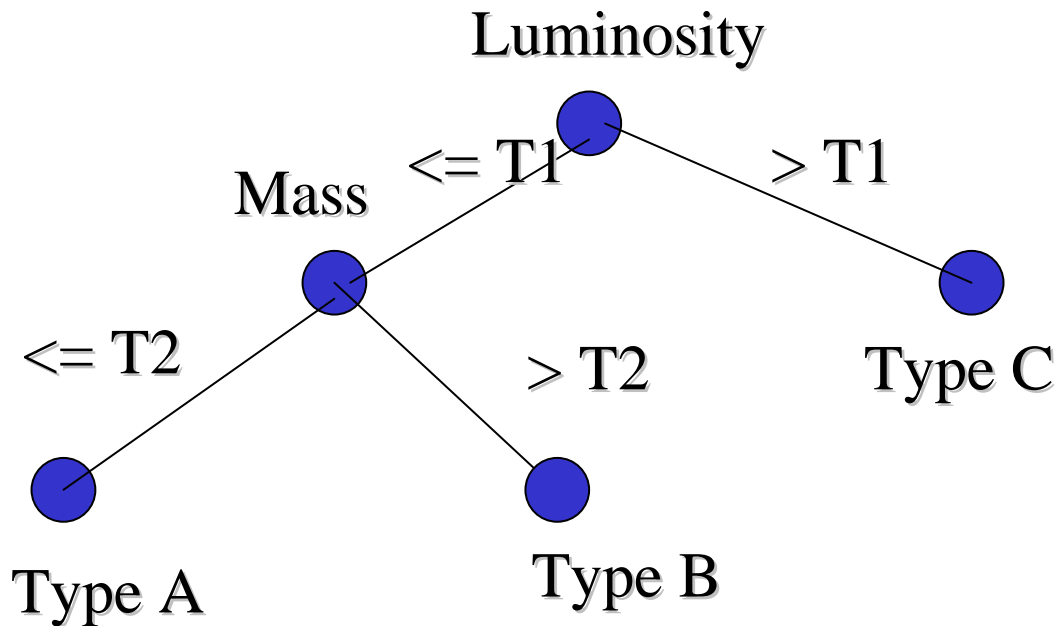
Version 1 CSE IIT, Kharagpur

# Lesson 35

## Rule Induction and Decision Tree - I

## 12.3 Decision Trees

Decision trees are a class of learning models that are more robust to noise as well as more powerful as compared to concept learning. Consider the problem of classifying a star based on some astronomical measurements. It can naturally be represented by the following set of decisions on each measurement arranged in a tree like fashion.



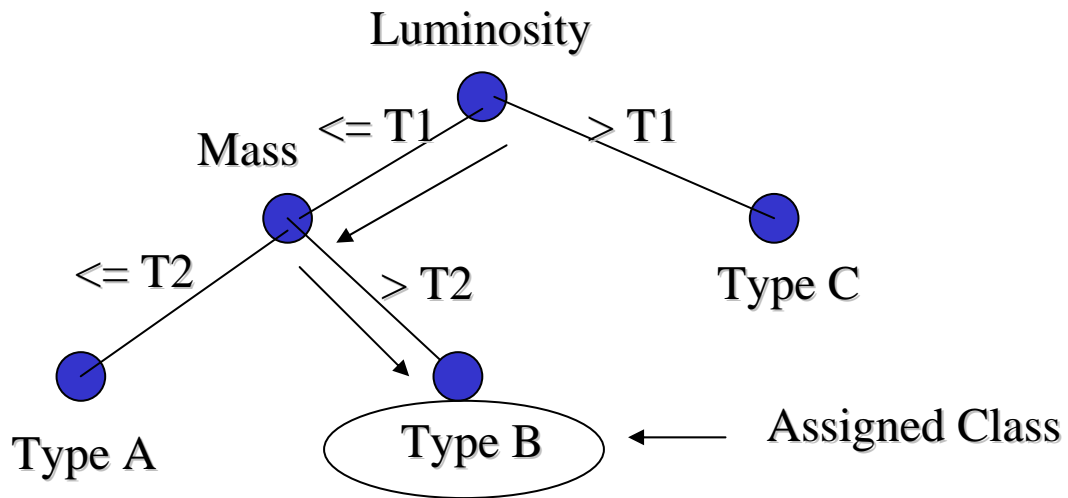
### 12.3.1 Decision Tree: Definition

- A decision-tree learning algorithm approximates a target concept using a tree representation, where each internal node corresponds to an attribute, and every terminal node corresponds to a class.
- There are two types of nodes:
  - Internal node.- Splits into different branches according to the different values the corresponding attribute can take. Example: luminosity  $\leq T1$  or luminosity  $> T1$ .
  - Terminal Node.- Decides the class assigned to the example.

### 12.3.2 Classifying Examples Using Decision Tree

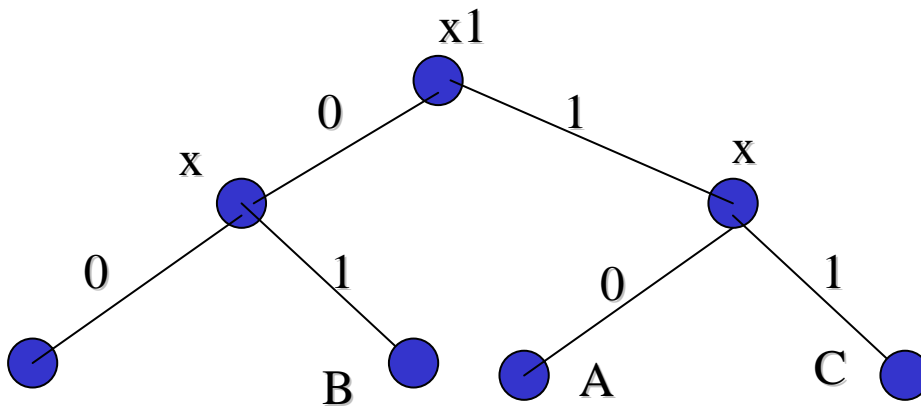
To classify an example  $X$  we start at the root of the tree, and check the value of that attribute on  $X$ . We follow the branch corresponding to that value and jump to the next node. We continue until we reach a terminal node and take that class as our best prediction.

$$X = (\text{Luminosity} \leq T1, \text{Mass} > T2)$$



Decision trees adopt a DNF (Disjunctive Normal Form) representation. For a fixed class, every branch from the root of the tree to a terminal node with that class is a conjunction of attribute values; different branches ending in that class form a disjunction.

In the following example, the rules for class A are:  $(\sim X1 \ \& \ \sim x2)$  OR  $(X1 \ \& \ \sim x3)$



### 12.3.3 Decision Tree Construction

There are different ways to construct trees from data. We will concentrate on the top-down, greedy search approach:

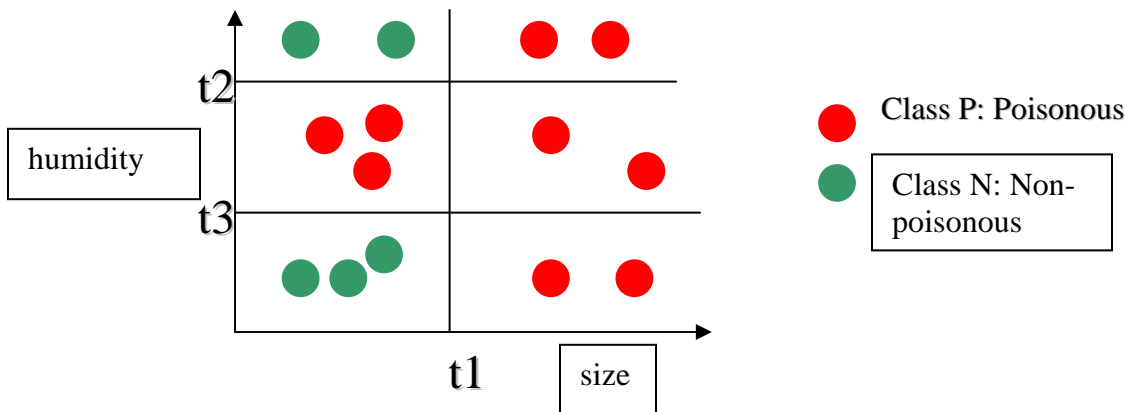
Basic idea:

1. Choose the best attribute  $a^*$  to place at the root of the tree.

2. Separate training set  $D$  into subsets  $\{D_1, D_2, \dots, D_k\}$  where each subset  $D_i$  contains examples having the same value for  $a^*$

3. Recursively apply the algorithm on each new subset until examples have the same class or there are few of them.

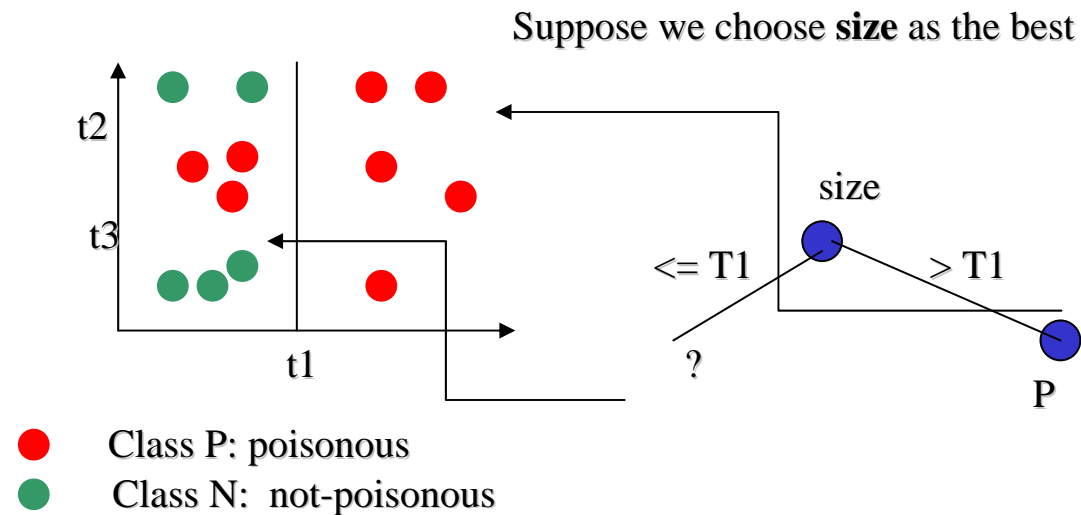
*Illustration:*



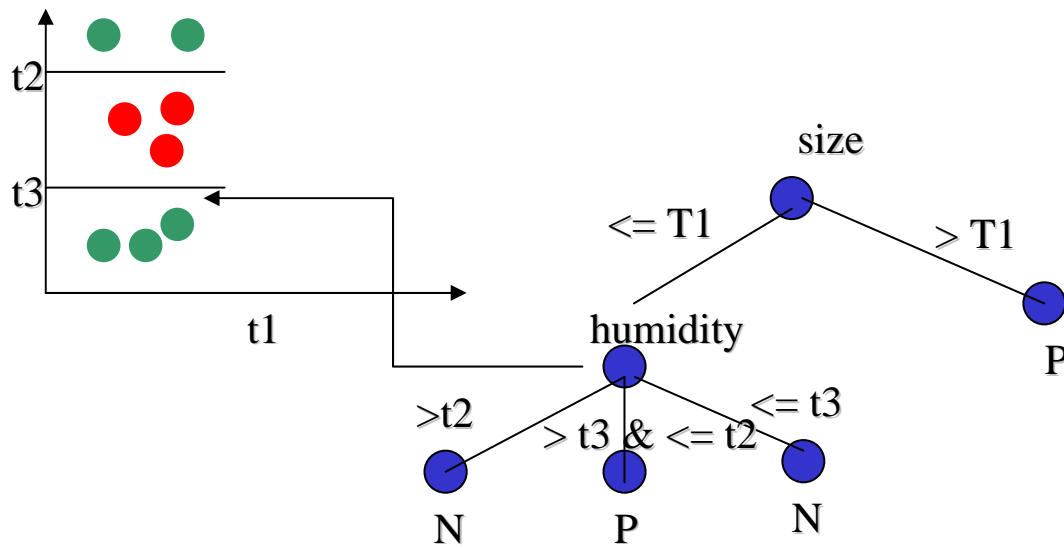
Attributes: size and humidity.

Size has two values:  $>t_1$  or  $\leq t_1$

Humidity has three values:  $>t_2$ ,  $(>t_3 \text{ and } \leq t_2)$ ,  $\leq t_3$



Suppose we choose **humidity** as the next best



#### Steps:

- Create a root for the tree
- If all examples are of the same class or the number of examples is below a threshold return that class
- If no attributes available return majority class
- Let  $a^*$  be the best attribute
- For each possible value  $v$  of  $a^*$ 
  - Add a branch below  $a^*$  labeled " $a = v$ "
  - Let  $S_v$  be the subsets of example where attribute  $a^* = v$
  - Recursively apply the algorithm to  $S_v$